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MA03

(9660/MA03) Unit P2 Pure Mathematics

Mark scheme

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Key to mark scheme abbreviations

M	Mark is for method
m	Mark is dependent on one or more M marks and is for method
A	Mark is dependent on M or m marks and is for accuracy
B	Mark is independent of M or m marks and is for method and accuracy
E	Mark is for explanation
√ or ft	Follow through from previous incorrect result
CAO	Correct answer only
CSO	Correct solution only
AWFW	Anything which falls within
AWRT	Anything which rounds to
ACF	Any correct form
AG	Answer given
SC	Special case
oe	Or equivalent
A2, 1	2 or 1 (or 0) accuracy marks
-x EE	Deduct x marks for each error
NMS	No method shown
PI	Possibly implied
SCA	Substantially correct approach
sf	Significant figure(s)
dp	Decimal place(s)

Q	Answer	Marks	Comments
1(a)(i)	$\left[\frac{dy}{dx} = \right] kx^4(3x^5 - 4)^7$	M1	k is an integer or product
	$\left[\frac{dy}{dx} = \right] 120x^4(3x^5 - 4)^7$	A1	Accept $5 \times 3 \times 8 \times x^4(3x^5 - 4)^7$
		2	

Q	Answer	Marks	Comments
1(a)(ii)	$\left[\frac{dy}{dx} = \right] \frac{p \times x^3(7x - 5) - qx^4}{(7x - 5)^2}$	M1	p, q integers
	$\left[\frac{dy}{dx} = \right] \frac{12x^3(7x - 5) - 21x^4}{(7x - 5)^2}$	A1	oe
	or $\left[\frac{dy}{dx} = \right] px^4(7x - 5)^{-2} + qx^3(7x - 5)^{-1}$	(M1)	
	$\left[\frac{dy}{dx} = \right] 3x^4(-1)(7)(7x - 5)^{-2} + (7x - 5)^{-1}12x^3$	(A1)	
	$\left[\frac{dy}{dx} = \frac{63x^4 - 60x^3}{(7x - 5)^2} \right]$		
		2	

Q	Answer	Marks	Comments
1(a)(iii)	$\frac{2x}{x^2} + 2y \frac{dy}{dx} = y + x \frac{dy}{dx}$	M1	Correct differentiation of y^2 or xy
	$\left[\frac{dy}{dx} = \right] \frac{y - \frac{2x}{x^2}}{2y - x}$	B1	Correct differentiation of $\ln(x^2)$
	$\left[\frac{dy}{dx} = \frac{xy - 2}{x(2y - x)} \right]$	A1	oe
		3	

Q	Answer	Marks	Comments
1(b)(i)	$\int \frac{x-6}{x^2-12x+5} dx = k \ln x^2-12x+5 $	M1	$k \neq 0$
	$= \frac{1}{2} \ln x^2-12x+5 \quad [+c]$	A1	oe Must be in terms of x condone brackets as moduli signs
		2	

Q	Answer	Marks	Comments
1(b)(ii)	$\left[\frac{d}{dx}(2x^2+3x-1) \right] = 4x+3$	B1	PI
	$\left[\int \frac{8x+6}{(2x^2+3x-1)^3} dx \right] = k(2x^2+3x-1)^{-2}$	M1	$k \neq 0$
	$= \frac{-1}{(2x^2+3x-1)^2} \quad [+c]$	A1	oe Must be in terms of x
		3	

	Question 1 Total	12	
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Q	Answer	Marks	Comments
2(a)(i)	$f(x) = 2^{-x} - 4 + 2x$ $f(1.8) = 2^{-1.8} - 4 + 3.6 = -0.1[12825]...$ $f(1.9) = 2^{-1.9} - 4 + 3.8 = 0.06[794]...$ Change of sign, $1.8 < \alpha < 1.9$	M1 A1	Or reverse Both values rounded or truncated to at least 1sf Must have both statement and interval in words or symbols or comparing 2 sides: at 1.8, $2^{-1.8} = 0.2[871].. < 0.4$; at 1.9, $2^{-1.9} = 0.26[79]... > 0.2$ Accuracy as before (M1) Conclusion as before (A1)
		2	

Q	Answer	Marks	Comments
2(a)(ii)	$2x = 4 - 2^{-x}$ $x = 2 - \frac{2^{-x}}{2}$ $x = 2 - 2^{-x-1}$ $x = 2 - 2^{-(x+1)}$	B1	AG Must be convincingly shown
		1	

Q	Answer	Marks	Comments
2(a)(iii)	$x_2 = 1.856$ $x_3 = 1.862$	B1 B1	AWRT 1.856 CAO
		2	

Q	Answer	Marks	Comments		
2(b)	<table border="1" style="width: 100%; text-align: center;"> <tr> <td style="width: 20%;">x</td> <td>y</td> </tr> </table>	x	y		
	x	y			
	1	$2^{-1} = 0.5$			
	1.75	$2^{-1.75} = 0.2973018$			
	2.5	$2^{-2.5} = 0.1767767$			
	3.25	$2^{-3.25} = 0.1051121$			
4.0	$2^{-4} = 0.0625$				
$\frac{1}{3} \times 0.75 [0.5 + 0.0625 + 4(0.2973018 + 0.1051121) + 2 \times 0.1767767]$ <p>0.6314</p>	<p>B1</p> <p>M1</p> <p>m1</p> <p>A1</p>	<p>All five correct x values (and no extra used) PI by five correct y values</p> <p>At least four correct y values in exact form or decimals, rounded or truncated to three dp or better (in table or formula) (PI by AWRT correct answer)</p> <p>Correct sub into formula with $h = 0.75$ OE and at least four correct y values either listed, with + signs, or totalled. (PI by AWRT correct answer)</p> <p>CAO, must see this value exactly and no error seen</p>			
		4			
	Question 2 Total	9			

Q	Answer	Marks	Comments
3(a)	Translation	B1	
	$\begin{bmatrix} -1 \\ 0 \end{bmatrix}$	B1	
	Stretch	B1	
	SF 0.5, parallel to y -axis	B1	
		4	

Q	Answer	Marks	Comments
3(b)		B1	Correct shape and position
		B1	Min at $(-1, 0.5)$ may be written as coordinates or indicated on the diagram
		B1	y -intercept as $(0, 0.9)$ AWRT oe may be written as coordinates or indicated on the diagram
		3	

Q	Answer	Marks	Comments
3(c)(i)	$\left[\frac{dx}{dy} = \right] \frac{1}{2} \sec y \tan y$	B1	oe
		1	

Q	Answer	Marks	Comments
3(c)(ii)	$\frac{dy}{dx} \left[= \frac{2}{\sec y \tan y} \right] = \frac{2 \cos^2 y}{\sin y}$ $= \frac{2(1 - \sin^2 y)}{\sin y}$	M1 A1	$\frac{dy}{dx} = \frac{1}{\frac{dx}{dy}}$ oe
		2	

	Question 3 Total	10	
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Q	Answer	Marks	Comments
4(a)	$[f(x)] \geq 0$	B1	Do not allow $x \geq 0$
		1	
Q	Answer	Marks	Comments
4(b)(i)	$fg(x) = \sqrt{1 - \frac{2}{x-1}}$	B1	oe eg $\sqrt{\frac{x-3}{x-1}}$
		1	
Q	Answer	Marks	Comments
4(b)(ii)	$\left[1 - \frac{2}{x-1} \geq 0 \right]$ $x \geq 3$ $x < 1$	B1 B1	oe oe
		2	
Q	Answer	Marks	Comments
4(b)(iii)	$1 - \frac{2}{x-1} = 9$ $[x-1 = -0.25]$ $x = 0.75$	M1 A1	Attempt to solve by eliminating square root. only
		2	
Q	Answer	Marks	Comments
4(c)(i)	$x = \sqrt{1 - \frac{2}{y-1}}$ $x^2 = 1 - \frac{2}{y-1}$ $h(x) = \frac{3-x^2}{1-x^2}$	M1 M1 A1	Interchange x and y Attempt to solve Allow $p = 3, q = 1$
		3	
Q	Answer	Marks	Comments
4(c)(ii)	$[9 - 3x^2 = 11 - 11x^2]$ $8x^2 = 2$ $x = [\pm]0.5$	M1 A1	At least one correct
		2	
Question 4 Total		11	

Q	Answer	Marks	Comments
5(a)	$[7 \cos \theta + 24 \sin \theta =]$ $R \cos \theta \cos \alpha + R \sin \theta \sin \alpha$ $R = 25$ $\alpha = 1.29$ $[7 \cos \theta + 24 \sin \theta = 25 \cos(\theta - 1.29)]$	M1 B1 A1	PI AWRT
		3	

Q	Answer	Marks	Comments
5(b)	$2 \operatorname{cosec} 4x + 2 \cot 4x = \frac{2}{\sin 4x} + \frac{2 \cos 4x}{\sin 4x}$ $= \frac{2 + 2(2 \cos^2 2x - 1)}{2 \sin 2x \cos 2x}$ $= \frac{4 \cos^2 2x}{2 \sin 2x \cos 2x}$ $= \frac{2 \cos 2x}{\sin 2x}$ $= \frac{\cos^2 x - \sin^2 x}{\sin x \cos x}$ $= \frac{\cos x}{\sin x} - \frac{\sin x}{\cos x}$ $= \cot x - \tan x$	M1 A1 M1 A1	Correct use of both double angle formulae Correct use of both double angle formulae AG no errors seen
		4	

Q	Answer	Marks	Comments
5(c)	$5(\sec^2 Y - 1) = 7 - 4 \sec Y$ $5 \sec^2 Y + 4 \sec Y - 12 = 0$ $(5 \sec Y - 6)(\sec Y + 2) [= 0]$ $\sec Y = -2, \frac{6}{5}$ $\left[\cos Y = \frac{5}{6}, -0.5 \right]$ $Y = 0.585, -0.585, 5.697, 6.868, 2.094,$ $4.188\dots, 8.377\dots$ $y = 0.59, 1.35, 1.93, 2.69$ <p>or</p> $5 \frac{\sin^2 Y}{\cos^2 Y} = 7 - \frac{4}{\cos Y}$ $5(1 - \cos^2 Y) = 7 \cos^2 Y - 4 \cos Y$ $12 \cos^2 Y - 4 \cos Y - 5 = 0$ $(6 \cos Y - 5)(2 \cos Y + 1) [= 0]$ $\cos Y = \frac{5}{6}, -0.5$	<p>M1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>[M1]</p> <p>[A1]</p>	<p>Correct use of trig identity PI</p> <p>Both values correct</p> <p>For any of these values, or rounded or truncated to 2 dp PI</p> <p>Sight of any of these values</p> <p>All 4 correct and no extras in interval (ignore answers outside interval)</p>
		5	
	Question 5 Total	12	

Q	Answer	Marks	Comments
6(a)	$4(0.5)^3 + a(0.5)^2 + b \times 0.5 + c = 0$ $4(1.5)^3 + a(1.5)^2 + b \times 1.5 + c = 15$	M1	One correct substitution
	$4((1.5)^3 - (0.5)^3) + a((1.5)^2 - (0.5)^2)$ $+ b(1.5 - 0.5) = 15$ or $a + 2b + 4c = -2$ $9a + 6b + 4c = 6$ $13 + 2a + b = 15$ or $8a + 4b = 8$ leading to $2a + b = 2$	m1	Attempt to eliminate c
		A1	AG no errors seen
		3	

Q	Answer	Marks	Comments
6(b)	$4(-0.5)^3 + a(-0.5)^2 + b \times (-0.5) + c = 9$	M1	Correct substitution
	$a - 2b + 4c = 38$ $4b = -40 \Rightarrow b = -10$	m1	Attempt to solve simultaneous equations in a , b and c
	$a = 6, c = 3$	A1	All 3 values correct
	$f(x) = 4x^3 + 6x^2 - 10x + 3$ $[f(-1.5)] = 18$	B1	
		4	

	Question 6 Total	7	
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Q	Answer	Marks	Comments
7(a)	$\frac{dx}{dt} = \frac{2t-1-2t}{(2t-1)^2}$ or $(-t)(2t-1)^{-2} + (2t-1)^{-1}$	M1	oe Either derivative correct
	$\frac{dy}{dt} = 2 - \frac{1}{2\sqrt{t}}$	A1	oe Both correct
	$\frac{dy}{dx} = -\frac{(2t-1)^2(4\sqrt{t}-1)}{2\sqrt{t}}$	m1	
	$t = 1, \frac{dy}{dx} = -\frac{3}{2}, x = 1, y = 1$	A1	All correct PI
	Equation of normal: $y - 1 = \frac{2}{3}(x - 1)$	M1	Correct attempt to find <i>their</i> normal
$3y - 2x = 1$	A1	Allow $p = 3, q = -2, r = 1$, Allow integer multiples	
		6	

Q	Answer	Marks	Comments
7(b)(i)	$x + y = 2e^{2m}$	M1	Both correct
	$x - y = 2e^{-2m}$		
	$\frac{x+y}{2} = \frac{2}{x-y}$	m1	Attempt to eliminate m
	$x^2 = y^2 + 4$	A1	
	or		
$x^2 = (e^{2m})^2 + (e^{-2m})^2 + 2$	[M1]	Either equation correct	
$y^2 = (e^{2m})^2 + (e^{-2m})^2 - 2$	[m1]	Both correct	
$x^2 = y^2 + 4$	[A1]		
		3	

Q	Answer	Marks	Comments
7(b)(ii)	$\left[\begin{array}{l} x + y = 2e^{kn} \quad x - y = 2e^{-kn} \\ \frac{x + y}{2} = \frac{2}{x - y} \\ x^2 = y^2 + 4 \end{array} \right]$	B1ft	oe
		1	

Q	Answer	Marks	Comments
7(c)	$\begin{aligned} x^2 &= a^2 \sin^2 \theta + b^2 \cos^2 \theta + 2ab \cos \theta \sin \theta \\ y^2 &= a^2 \cos^2 \theta + b^2 \sin^2 \theta - 2ab \cos \theta \sin \theta \\ x^2 + y^2 &= a^2 (\sin^2 \theta + \cos^2 \theta) + b^2 (\cos^2 \theta + \sin^2 \theta) \\ x^2 + y^2 &= a^2 + b^2 \end{aligned}$ <p>or</p> $\begin{aligned} ax - by &= \sin \theta (a^2 + b^2) \\ ay + bx &= \cos \theta (a^2 + b^2) \\ \left(\frac{ax - by}{a^2 + b^2} \right)^2 + \left(\frac{ay + bx}{a^2 + b^2} \right)^2 &= 1 \\ \left[(ax - by)^2 + (ay + bx)^2 = (a^2 + b^2)^2 \right] \end{aligned}$	<p>M1</p> <p>m1</p> <p>A1</p> <p>[M1]</p> <p>[m1] [A1]</p>	<p>Squaring one expression (condone one slip)</p> <p>Attempt to eliminate θ</p> <p>oe</p> <p>One expression in either $\sin \theta$ or $\cos \theta$ (condone one slip)</p> <p>Attempt to eliminate θ</p>
		3	

	Question 7 Total	13	
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Q	Answer	Marks	Comments
8(a)	$\frac{dP}{dt} = kP$ [3000 = $k \times 1000000$]	M1	
	$\frac{dP}{dt} = 0.003P$	A1	oe
		2	

Q	Answer	Marks	Comments
8(b)	$2x \frac{dy}{dx} = 4 - y^2$		
	$\int \frac{dy}{4 - y^2} = \int \frac{dx}{2x}$	B1	PI Correctly separate variables
	$\frac{1}{4 - y^2} = \frac{A}{2 - y} + \frac{B}{2 + y}$	M1	Using partial fractions
	$1 = A(2 + y) + B(2 - y)$		
	$A = 0.25, B = 0.25$	A1	Both correct
	$\frac{1}{4} \int \frac{1}{2 - y} + \frac{1}{2 + y} dy = \frac{1}{2} \int \frac{dx}{x}$ $-\ln(2 - y) + \ln(2 + y) = 2 \ln x + \ln A$ (or $+c$)	m1	Correct integration (at least 3 terms correct)
$\ln \frac{2 + y}{2 - y} = \ln Ax^2$			$\int \frac{dy}{4 - y^2} = \frac{1}{4} \ln \left \frac{2 + y}{2 - y} \right $ scores M1A1m1
$Ax^2 = \frac{2 + y}{2 - y}$	m1	Eliminating 'ln' from <i>their</i> equation – must have scored M1m1	
$(1, 1) \Rightarrow A = 3$ $3x^2(2 - y) = 2 + y$ $y = \frac{2(3x^2 - 1)}{(3x^2 + 1)}$	A1	ACF	or $(1, 1) \Rightarrow c = \pm \frac{1}{4} \ln 3$
		6	

	Question 8 Total	8	
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Q	Answer	Marks	Comments
9(a)	$\frac{dy}{dx} = Ax^{0.5}e^{-0.5x} + Bx^{-0.5}e^{-0.5x}$	M1	Equating to 0 and attempt to solve
	$\frac{dy}{dx} = x^{0.5}(-0.5)e^{-0.5x} + 0.5x^{-0.5}e^{-0.5x}$	A1	
	$x^{0.5}(-0.5)e^{-0.5x} + 0.5x^{-0.5}e^{-0.5x} = 0,$ $0.5x^{0.5} = 0.5x^{-0.5}$	m1	
	$x = 1$ $(1, e^{-0.5})$	A1	
		4	

Q	Answer	Marks	Comments
9(b)	$V = \pi \int_1^2 (\sqrt{x}e^{-0.5x})^2 dx$	B1	PI by final answer
	$\int xe^{-x} dx = -xe^{-x} - \int -e^{-x} dx$	M1	Use of parts formula
	$= -xe^{-x} - e^{-x}$	A1	
	$\int_1^2 = [\pi] (-xe^{-x} - e^{-x})_1^2$		
	$= [\pi] ((-2e^{-2} - e^{-2}) - (-e^{-1} - e^{-1}))$	m1	Correct substitution of <i>their</i> 1, 2 into <i>their</i> expression in the form $axe^{-x} + be^{-x}$
$= \pi \left(\frac{2}{e} - \frac{3}{e^2} \right)$	A1	Allow $a = 2, b = -3$	
		5	

	Question 9 Total	9	
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Q	Answer	Marks	Comments
10	$\frac{du}{d\theta} = \cos \theta$ $\left[\int \frac{\cos^3 \theta}{(1 + \sin \theta)^{1.5}} d\theta = \int \frac{1 - (u - 1)^2}{(u)^{1.5}} du \right]$ $\int \frac{2u - u^2}{(u)^{1.5}} du$ $= \int 2u^{-0.5} - u^{0.5} du$ $= 4u^{0.5} - \frac{2}{3}u^{1.5} \quad [+c]$ $[\theta]_0^{\frac{\pi}{2}} = [u]_1^2$ $\left[\int_0^{\frac{\pi}{2}} \frac{\cos^3 \theta}{(1 + \sin \theta)^{1.5}} d\theta = \left(4u^{0.5} - \frac{2}{3}u^{1.5} \right)_1^2 \right]$ $= \left(4 \times 2^{0.5} - \frac{2}{3} \times 2^{1.5} \right) - \left(4 - \frac{2}{3} \right)$ $= \frac{8}{3} \times 2^{0.5} - \frac{10}{3}$ $= \frac{2}{3}(4\sqrt{2} - 5)$	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1ft</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>oe PI</p> <p>All in terms of u, condone omission of du</p> <p>Must see du here, or earlier</p> <p>$Au^{0.5} + Bu^{1.5}$</p> <p>Correct integration</p> <p>Change of limits, maybe seen earlier (may change back to θ and not change limits)</p> <p>Correct substitution of <i>their</i> limits into <i>their</i> expression of the form $Au^{0.5} + Bu^{1.5}$</p> <p>Allow $p = 4, q = -5$</p>
		8	
	Question 10 Total	8	

Q	4Answer	Marks	Comments
11(a)	$f(x) = \frac{A}{(3-x)} + \frac{B}{(3-x)^2} + \frac{C}{(1-3x)}$ $7x^2 - 17x + 12 = A(3-x)(1-3x) + B(1-3x) + C(3-x)^2$ $x = 3, 24 = -8B, B = -3$ $x = \frac{1}{3}, \frac{64}{9} = \frac{64}{9}C, C = 1$ $x = 0, 12 = 3A + B + 9C, A = 2$ $f(x) = \frac{2}{(3-x)} - \frac{3}{(3-x)^2} + \frac{1}{(1-3x)}$	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>Correctly eliminating fractions</p> <p>Attempt at finding one constant</p> <p>Two constants correct</p> <p>Allow $A = 2, B = -3, C = 1$</p> <p>Allow equivalent methods</p>
		4	

Q	Answer	Marks	Comments
11(b)	$(3-x)^{-1} = \frac{1}{3} \left(1 - \frac{1}{3}x\right)^{-1}$ $= \frac{1}{3} + \frac{1}{9}x + \frac{1}{27}x^2$	<p>M1</p> <p>A1</p>	
		2	

Q	Answer	Marks	Comments
11(c)	$(3-x)^{-2} = \left(\frac{1}{3}\right)^2 \left(1 + \frac{2}{3}x + \frac{1}{3}x^2\right)$ $(1-3x)^{-1} = 1 + 3x + 9x^2$ $f(x):$ $2\left(\frac{1}{3} + \frac{1}{9}x + \frac{1}{27}x^2\right) - 3 \times \frac{1}{9} \left(1 + \frac{2}{3}x + \frac{1}{3}x^2\right) + 1(1 + 3x + 9x^2)$ $f(x) = \frac{4}{3} + 3x + \frac{242}{27}x^2$ $\left[D = \frac{4}{3}, E = 3, F = \frac{242}{27} \right]$	<p>M1</p> <p>A1</p> <p>m1</p> <p>A1</p>	<p>oe either expansion correct</p> <p>Both correct</p> <p>Correct substitutions of <i>their</i> expansions into <i>their three term part (a)</i></p>
		4	

	Question 11 Total	10	
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	Answer	Marks	Comments
12(a)	$[l_1: \mathbf{r} =] \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix} + \lambda \begin{bmatrix} 3 \\ -1 \\ -4 \end{bmatrix}$	B1	oe $[l_1: \mathbf{r} =] \begin{bmatrix} 5 \\ -2 \\ -1 \end{bmatrix} + \lambda \begin{bmatrix} 3 \\ -1 \\ -4 \end{bmatrix}$
		1	

Q	Answer	Marks	Comments
12(b)(i)	$2 + 3\lambda = -2 - \mu$ $-1 - \lambda = 5 - 2\mu$ $[7\lambda = -14 \Rightarrow \lambda = -2,] \mu = 2$ $[z: 3 - 4 \times -2 = 11 = 7 + 2k] k = 2$	M1 A1 A1	Both equations correct, ft from (a)
		3	2

Q	Answer	Marks	Comments
12(b)(ii)	$(-4, 1, 11)$	B1	
		1	

Q	Answer	Marks	Comments
12(c)	Coords of $D(-2 - d, 5 - 2d, 7 + 2d)$ $\overrightarrow{CD} = \begin{bmatrix} -5 - d \\ 1 - 2d \\ 3 + 2d \end{bmatrix}$ $\begin{bmatrix} -5 - d \\ 1 - 2d \\ 3 + 2d \end{bmatrix} \cdot \begin{bmatrix} -1 \\ -2 \\ 2 \end{bmatrix} [= 0]$ $9d = -9 \Rightarrow d = -1$ Coords of $D(-1, 7, 5)$ $\text{Dist} = \sqrt{(-1-3)^2 + (7-4)^2 + (5-4)^2}$ $= \sqrt{26}$	B1ft M1 m1 A1 M1 A1	Ft their 'k' in (b)(i) oe Seen or used, Ft their 'D' Correct use of dot product with their CD and their k Must have scored m1
		6	

	Question 12 Total	11	
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